



יישומים של מדידות פאזריות במערכות הספק ורשתות  
חשמל  
Applications of PMU for Monitoring and Control in  
Power Systems

Prof. Aleksei Korolev, SATEC Ltd.



# Prof. Aleksei Korolev

CTO, SATEC LTD.

Since 2022  
SATEC Ltd

CTO

2011 - 2022  
ETAP Systems LTD, authorized representative of ETAP in Russia

Head of engineering group  
Conducted 15+ ETAP Workshops

2017 - 2023  
Russian University of Transport (MIIT)

Visiting professor,  
15+ graduate theses

 <https://www.linkedin.com/in/aleksei-korolev-860ba148/>

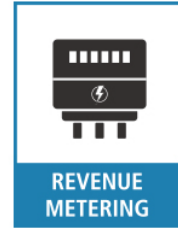
 <https://www.researchgate.net/profile/Aleksei-Korolev-5>

 <https://scholar.google.com/citations?user=ywLGklkAAAAJ&hl=en>


 <https://orcid.org/0000-0002-2424-3758>

# SATEC Ltd.

## Israel, Jerusalem

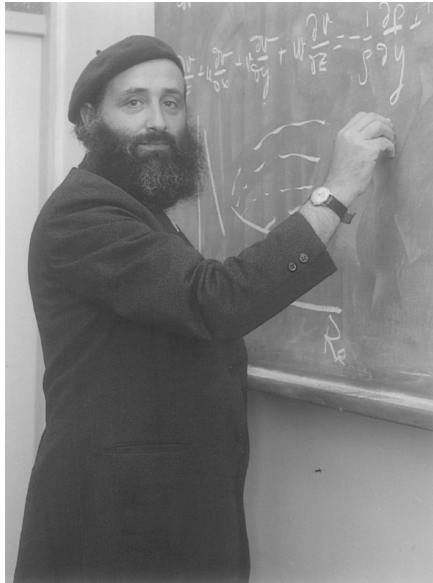


- **Founded in 1987**
- **International Company**
- **Activities in more than 70 countries**
- **Market leader in power quality and power metering**
- **One of the first digital power meters**

 Manufacturing, Sales & Support

 Sales & Support

# THE SATEC LEGACY



**Prof. German Branover,  
The founder of SATEC**

His vision went beyond creating a profitable business for pioneering power analysis.

His focus was on employment for a wave of immigrants from the former Soviet Union to Israel in the early 1990s and of whom many were highly educated engineers.

As an immigrant himself, who is also a renowned professor of physics, he appreciated the need for a fitting work environment. However, more than just promoting a social project, Prof. Branover wanted to demonstrate that there was also a **profitable incentive in this approach.**

Thirty six years later, SATEC has proven to be everything Prof. Branover expected of it and much more. Being a home and family to many of the said immigrants, SATEC benefitted beyond measure from these experts who developed and implemented the most innovative ideas in power measurement and telemetry, always affirming SATEC's place as a **global front-runner.**





# What is PMU?

**PMU** is Phasor Measurement Unit  
(**Synchrophasor**)

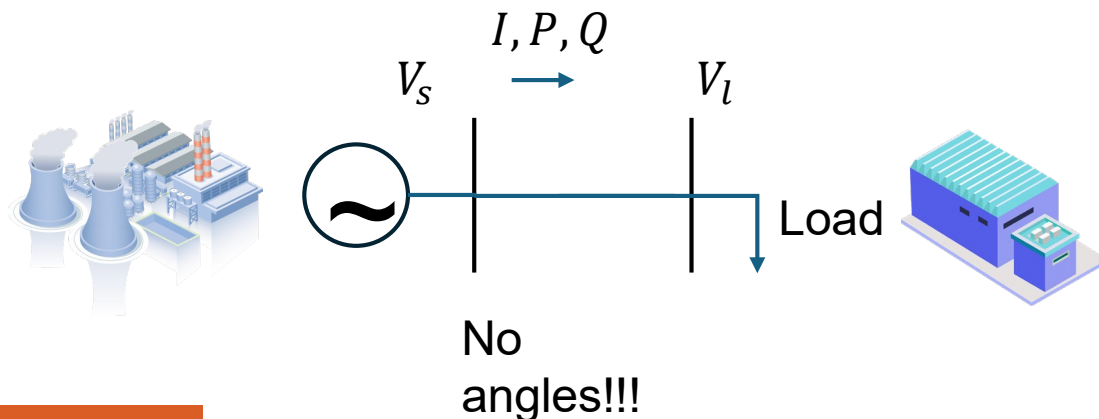
But what does it mean exactly?



# Phasors in AC networks

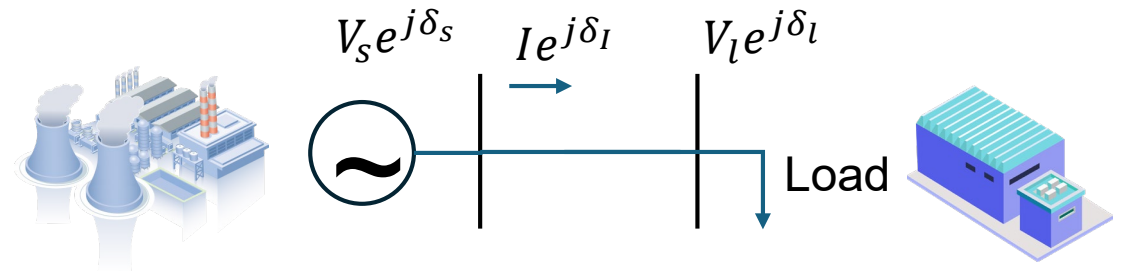
## Regular measurements (meters, PQanalyzers)

- Voltages, currents as RMS values using IEC 61000-4-30 and IEC 61000-4-7
- No phase angles
- Difficult to analyze the behavior of the network



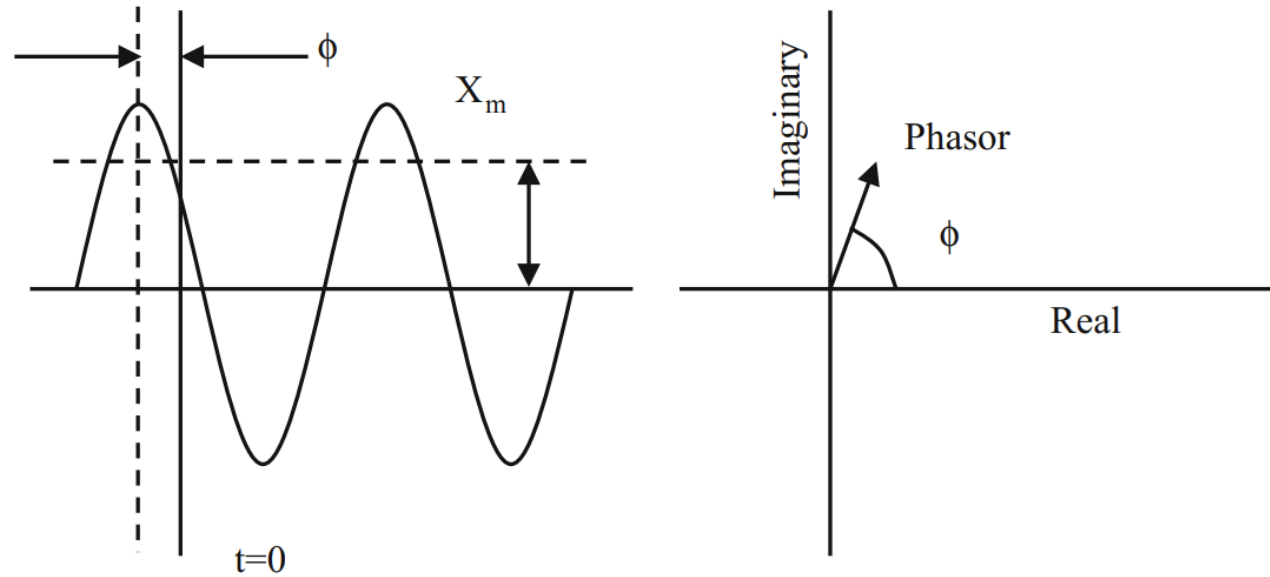
## Fundamentals of Electrical Engineering, Power Systems Stability and Control

- Circuit equivalents
- Voltage and current sources as complex values
- Currents in branches as complex values
- Voltages in buses as complex values
- Full analysis of the network



# Phasor definition

$$x(t) = X_m \cos(\omega t + \phi) \quad x(t) \leftrightarrow \mathbf{X} = \left( X_m / \sqrt{2} \right) e^{j\phi} = \left( X_m / \sqrt{2} \right) [\cos \phi + j \sin \phi]$$

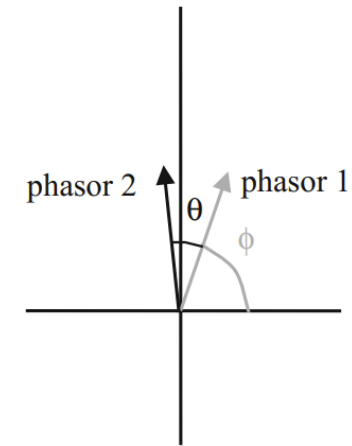
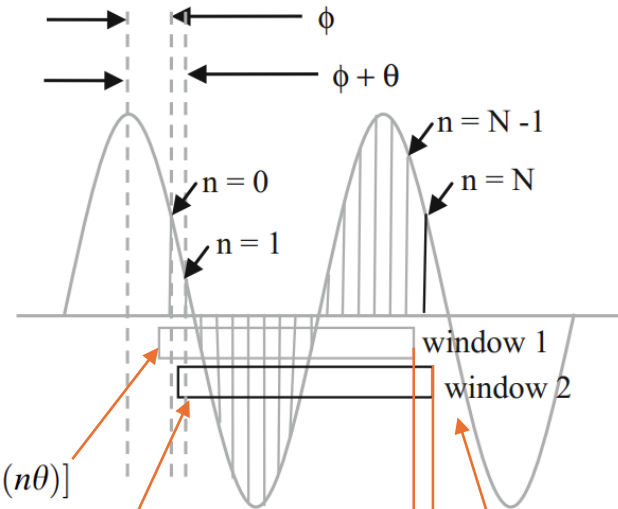


# Phasor calculation

Simplified explanation

$$X^{N-1} = \frac{\sqrt{2}}{N} \sum_{n=0}^{N-1} x_n [(\cos(n\theta) - j \sin(n\theta))]$$

$$X^N = \frac{\sqrt{2}}{N} \sum_{n=0}^{N-1} x_{n+1} [(\cos(n\theta) - j \sin(n\theta))]$$

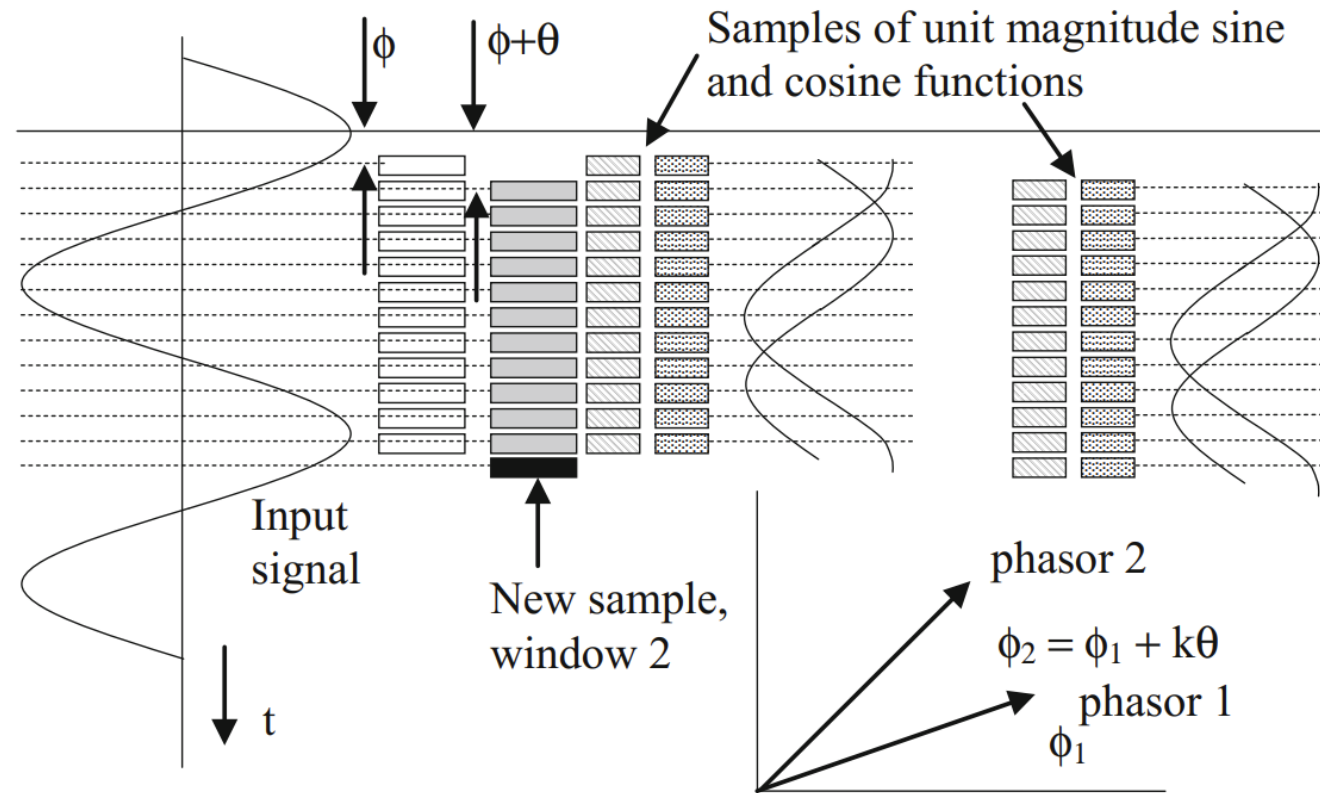


Sliding window

1 sample



# Phasor calculation



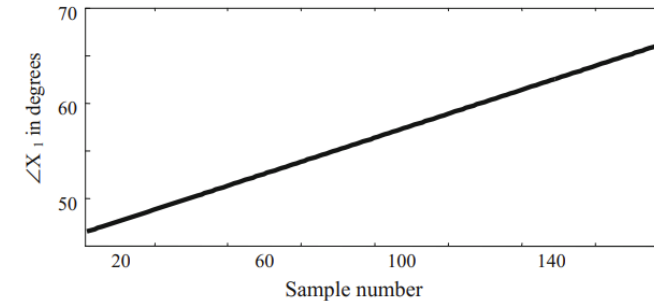
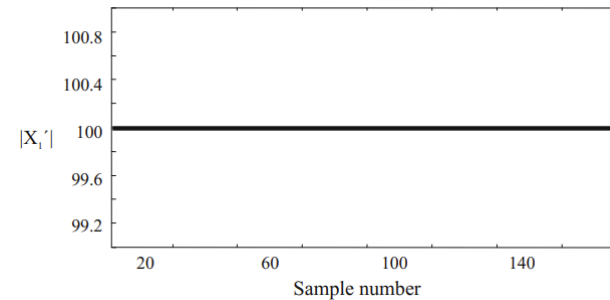
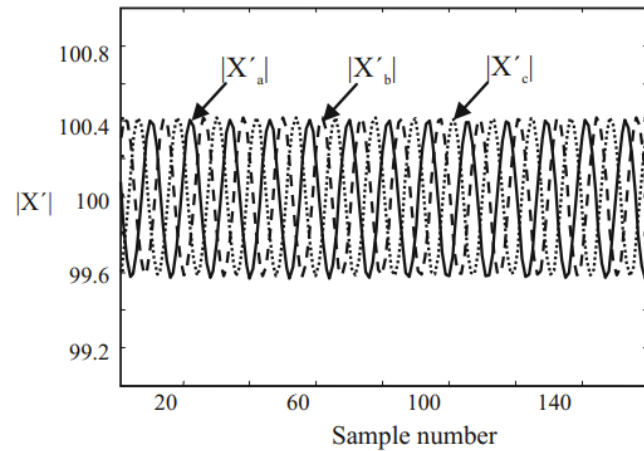
# Constant rotation



[https://www.linkedin.com/posts/epassa\\_engineering-electrical-electricalengineering-activity-7212100699910758402-uVqP/?utm\\_source=share&utm\\_medium=member\\_desktop](https://www.linkedin.com/posts/epassa_engineering-electrical-electricalengineering-activity-7212100699910758402-uVqP/?utm_source=share&utm_medium=member_desktop)

# Frequency and ROCOF

## Frequency and ROCOF

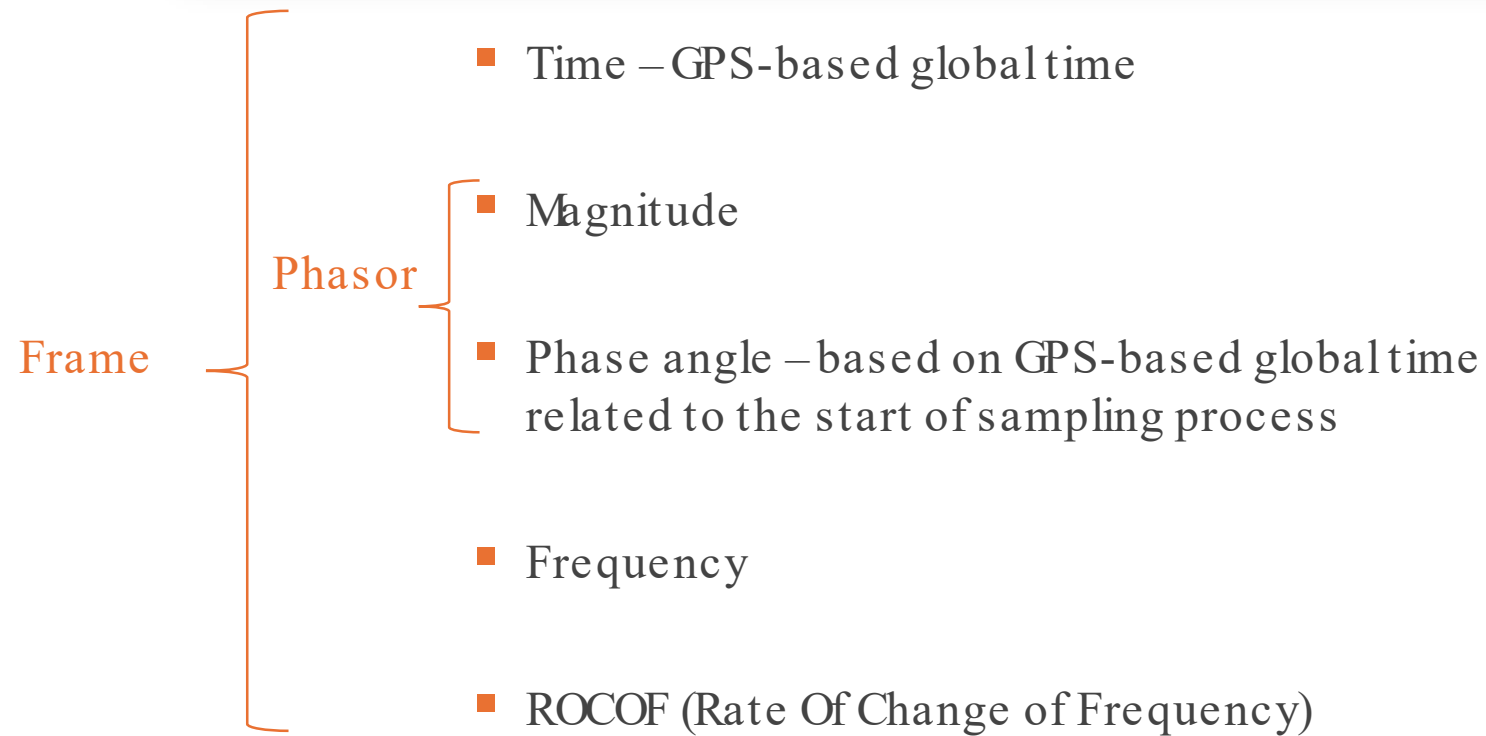


$$f(t) = \frac{1}{2\pi} \frac{d\psi(t)}{dt}$$

$$\text{ROCOF}(t) = \frac{df(t)}{dt}$$

Linear change = constant frequency

# Phasor frame



## Accuracy

- Magnitude – 0.1%
- Angle  
1  $\mu$ s in time  
0.02° for 60 Hz

### 3.2 Special terms

**ANSI C37.118.1-2011** **frame:** In this standard, a *data frame* or a *frame of data* is a set of synchrophasor, frequency, and ROCOF measurements that corresponds to the same time stamp. The term *frame* is used to differentiate it from *samples*, which are understood as points on an analog waveform.

# Phasor requirements

## ANSI C37.118.1-2011

**Table 1—Required PMU reporting rates**

System frequency	50 Hz			60 Hz					
Reporting rates ( $F_s$ —frames per second)	10	25	50	10	12	15	20	30	60

**In SATEC we do even more!**



# Main applications of PMU

1

## Preventing blackouts

Work with control and automation equipment

2

## Islanding

Validate voltage magnitudes and angles for sync  
Check power balances

3

## Grid operation

Voltage, power, frequency regulation

4

## Grid restoration

Stability assessment when add new loads and generation

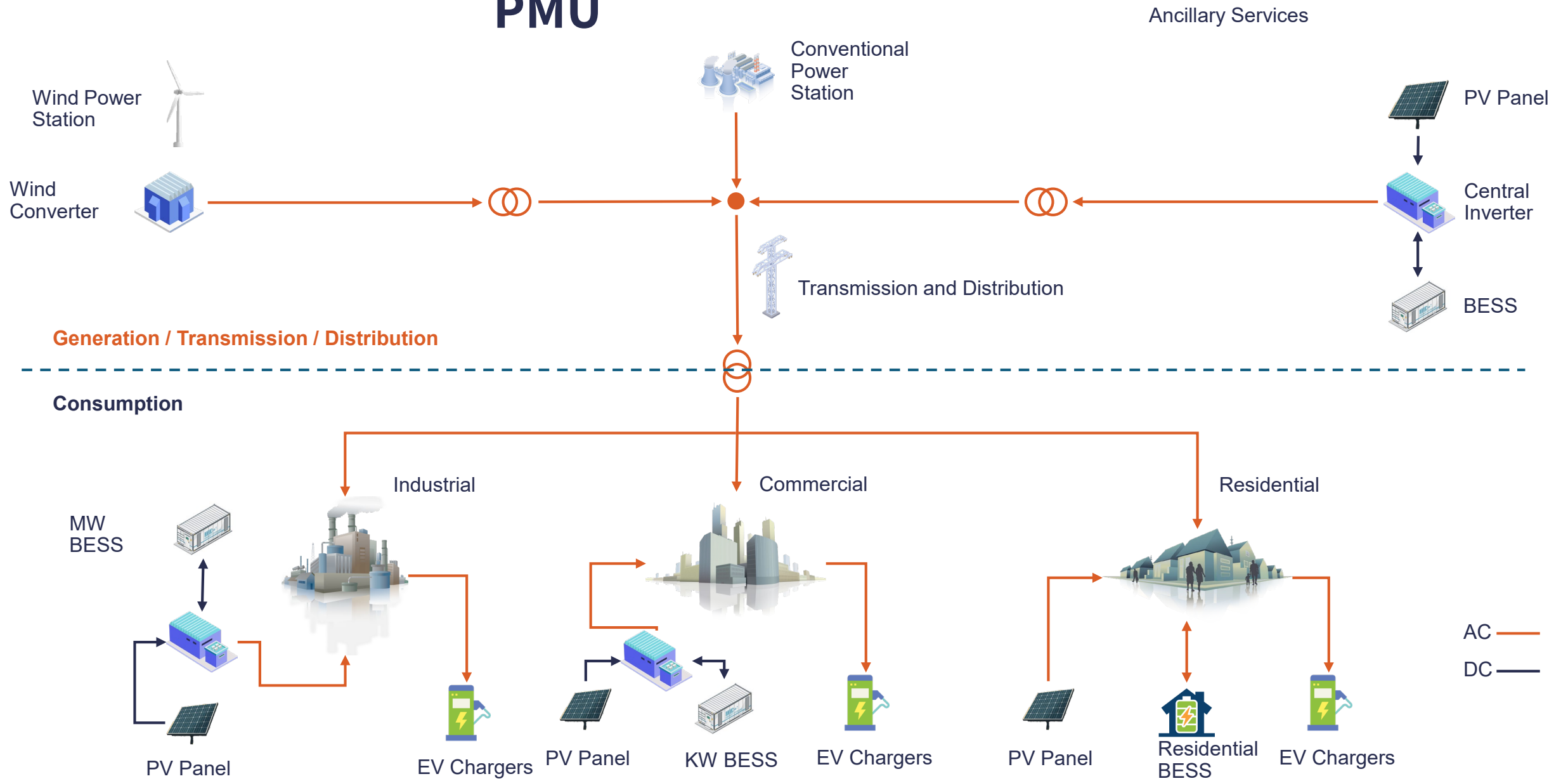
5

## Additional functions

Reserve assessment  
Forecasting  
Energy market operation



# Main applications of PMU



# Monitoring systems overview

Global types

SCADA

- You get only what you measure
- Analytics is limited

Model-based system

- **State Estimation**
- Analytics using both measurements and the model

Digital Twin



# Digital Twin- definition

**Digital Twin is the combination of a digital model of the real system and input/output channels connecting field measurement devices of the real system.**

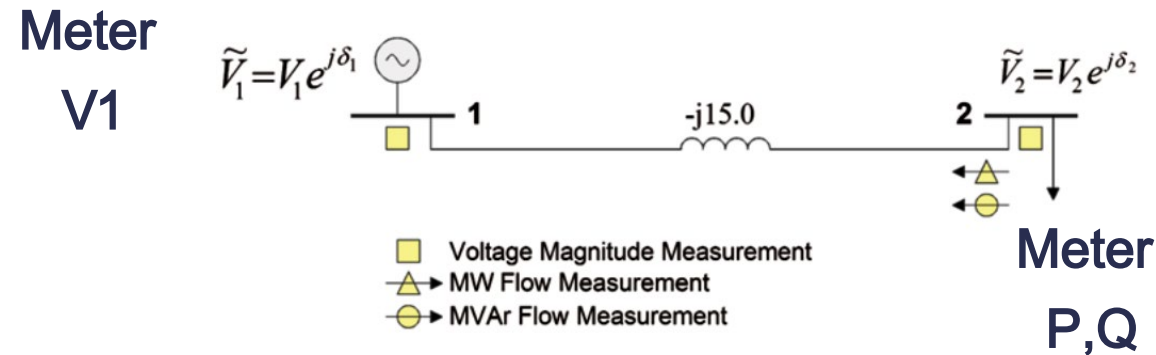


# State Estimation

## Early developments

F. Schweppe, J. Wildes, and D. Rom, "Power system static state estimation: Parts I, II, and III," Power Industry Computer Conference (PICA), Denver, Colorado June, 1969

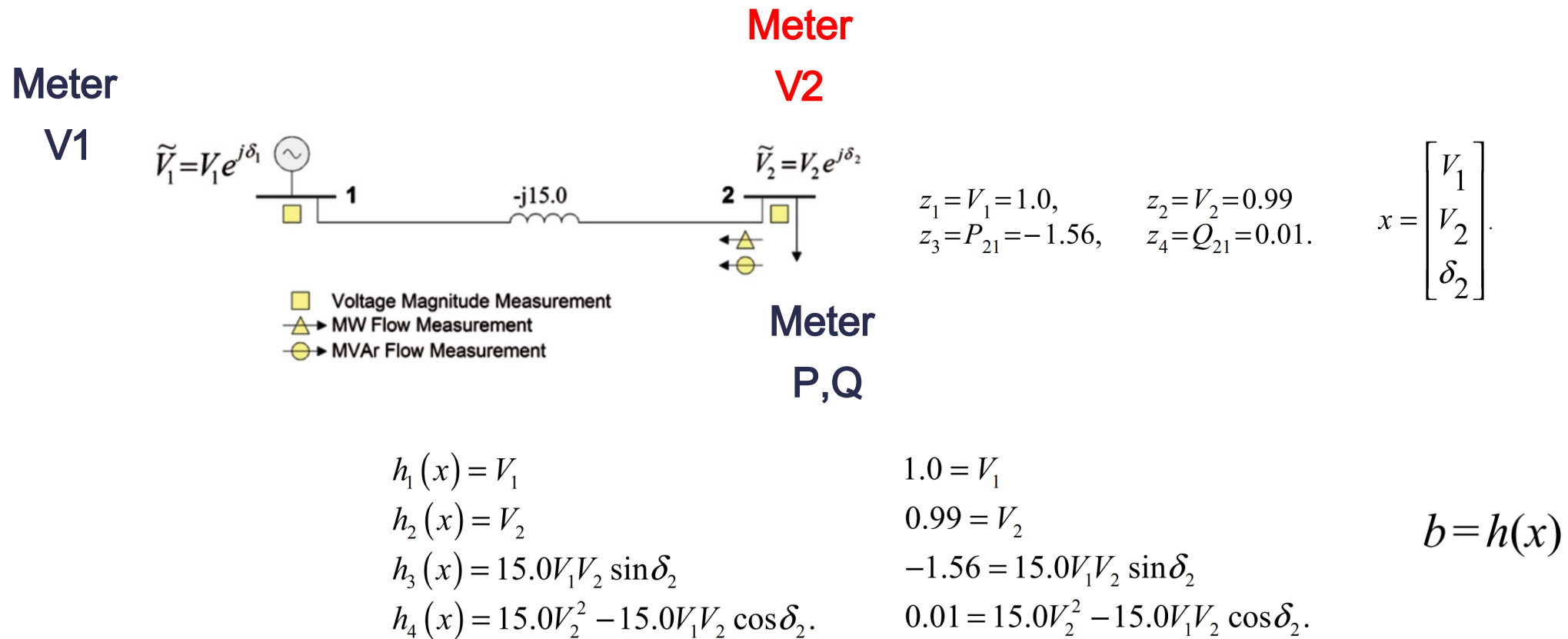
# Simple power system



$$\begin{cases} F_{P_k}(\theta, U) = 0 \\ F_{Q_k}(\theta, U) = 0 \end{cases}
 \begin{cases} \sum_n (U_k U_n (g_{kn} \cos(\theta_n - \theta_k) - b_{kn} \sin(\theta_n - \theta_k))) - P_k = 0 \\ \sum_n (U_k U_n (g_{kn} \sin(\theta_n - \theta_k) + b_{kn} \cos(\theta_n - \theta_k))) + Q_k = 0 \end{cases}
 \begin{bmatrix} \frac{\partial F_p}{\partial \theta} & \frac{\partial F_p}{\partial U} \\ \frac{\partial F_Q}{\partial \theta} & \frac{\partial F_Q}{\partial U} \end{bmatrix}
 \begin{bmatrix} \Delta \theta \\ \Delta U \end{bmatrix} = - \begin{bmatrix} F_p \\ F_Q \end{bmatrix}$$

2 variables, 2 equations – solvable system!

# State Estimation formulation



**3 variables, 4 equations – not a solvable system!**



# State Estimation formulation

## Least mean square method

Minimize the value

$$J = [h(x) - b]^T W [h(x) - b] \quad \frac{dJ}{dx} = \frac{d}{dx} [(Hx - b)^T W (Hx - b)] = 2H^T W (Hx - b) = 0 \quad \left. \frac{\partial h(x)}{\partial x} \right|_{x=x^0} = H$$

$$x = (H^T W H)^{-1} H^T W b$$

$$x^{v+1} = x^v - (H^T W H)^{-1} H^T W [h(x^v) - b]$$

Iterative estimation algorithm!

# Calculation example

$$H = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 15V_2 \sin \delta_2 & 15V_1 \sin \delta_2 & 15V_1 V_2 \cos \delta_2 \\ -15V_2 \cos \delta_2 & 30V_2 - 15V_1 \cos \delta_2 & 15V_1 V_2 \sin \delta_2 \end{bmatrix}$$

$$r^0 = h(x^0) - b = \begin{bmatrix} 0.0 \\ 0.0 \\ 1.56 \\ -0.1585 \end{bmatrix} \quad H(x^0) = \begin{bmatrix} 1.0 & 0.0 & 0.0 \\ 0.0 & 1.0 & 0.0 \\ 0.0 & 0.0 & 14.85 \\ -14.85 & 14.7 & 0.0 \end{bmatrix} \quad H^T H = \begin{bmatrix} 221.5225 & -218.295 & 0.0 \\ -218.295 & 217.09 & 0.0 \\ 0.0 & 0.0 & 220.5225 \end{bmatrix}$$

$$(H^T H)^{-1} H^T r^0 = \begin{bmatrix} 0.00538 \\ -0.00532 \\ 0.10505 \end{bmatrix} \quad x^1 = \begin{bmatrix} 1.0 \\ 0.99 \\ 0.0 \end{bmatrix} - \begin{bmatrix} 0.00538 \\ -0.00532 \\ 0.10505 \end{bmatrix} = \begin{bmatrix} 0.9946 \\ 0.9953 \\ -0.10505 \end{bmatrix}$$

$$r^1 = h(x^1) - b = \begin{bmatrix} -0.0054 \\ 0.0053 \\ 0.0030 \\ 0.0823 \end{bmatrix} \quad H(x^1) = \begin{bmatrix} 1.0 & 0.0 & 0.0 \\ 0.0 & 1.0 & 0.0 \\ -1.5655 & -1.5644 & 14.767 \\ -14.8472 & 15.0222 & -1.557 \end{bmatrix} \quad H^T H = \begin{bmatrix} 223.89 & -220.589 & -0.000647 \\ -220.589 & 229.114 & -46.4911 \\ -0.000647 & -46.4911 & 220.489 \end{bmatrix}$$

$$(H^T H)^{-1} H^T r^1 = \begin{bmatrix} -0.0027869 \\ 0.0027593 \\ 0.00019540 \end{bmatrix} \quad x^2 = \begin{bmatrix} 0.99741 \\ 0.99255 \\ -0.10525 \end{bmatrix}$$

$$r_1 = V_1 - 1.0 = -0.00259$$

$$r_2 = V_2 - 0.99 = -0.00256$$

$$r_3 = 15.0V_1 V_2 \sin \delta_2 + 1.56 = 0.00000614$$

$$r_4 = 15.0V_2^2 - 15.0V_1 V_2 \cos \delta_2 - 0.01 = 0.0000566$$

**The system has been estimated!**



# PMU-based State Estimation

## Linear estimation!

$$x = (H^T W H)^{-1} H^T W b$$

- Better accuracy
- Robust (no fear of divergence)
- It is faster
- More applications



# Power systems analysis

## Power Flow equations

- Number of equations equals to number of variables – system of equations
- Assumptions about element impedances

## State Estimation

- Overdetermined system
- Calculations with uncertainty



# Uncertainties everywhere

- Metering devices uncertainty
- Current/voltage sensors uncertainties
- Power System elements impedances uncertainties

## IEC 60076 Power transformers

Rated kVA	%Z tolerance
< 500 kVA	$\pm 10\%$
> 2 MVA	$\pm 5\%$



# Digital Twin and PMU

## Applications

- Virtual measurements using State Estimation
- **Equipment Diagnostics**
- Optimization
- Transient Analysis
- Load Shedding
- Fault Location Detection



# PM180 PMU + PQM and more



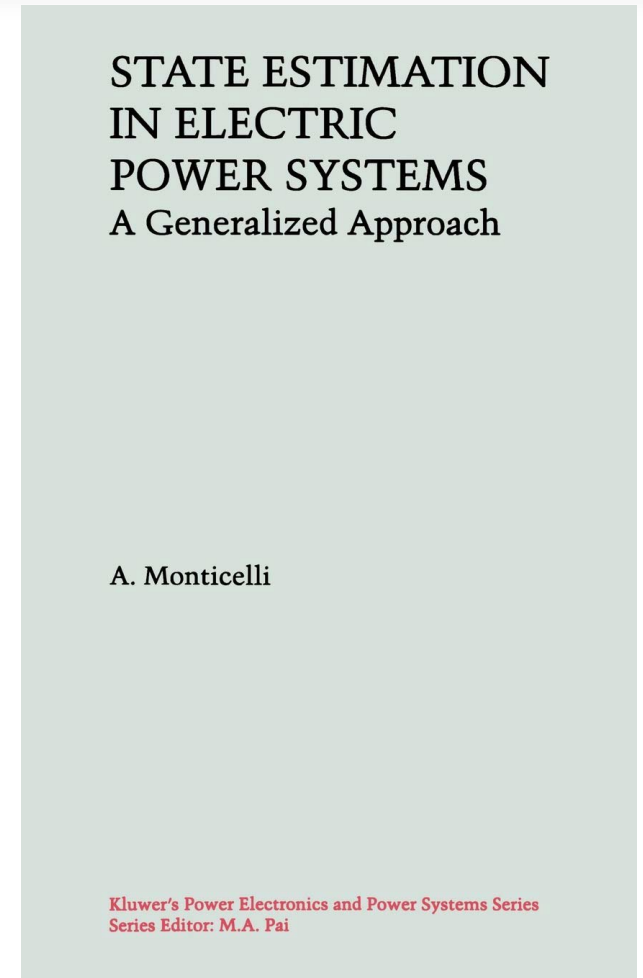
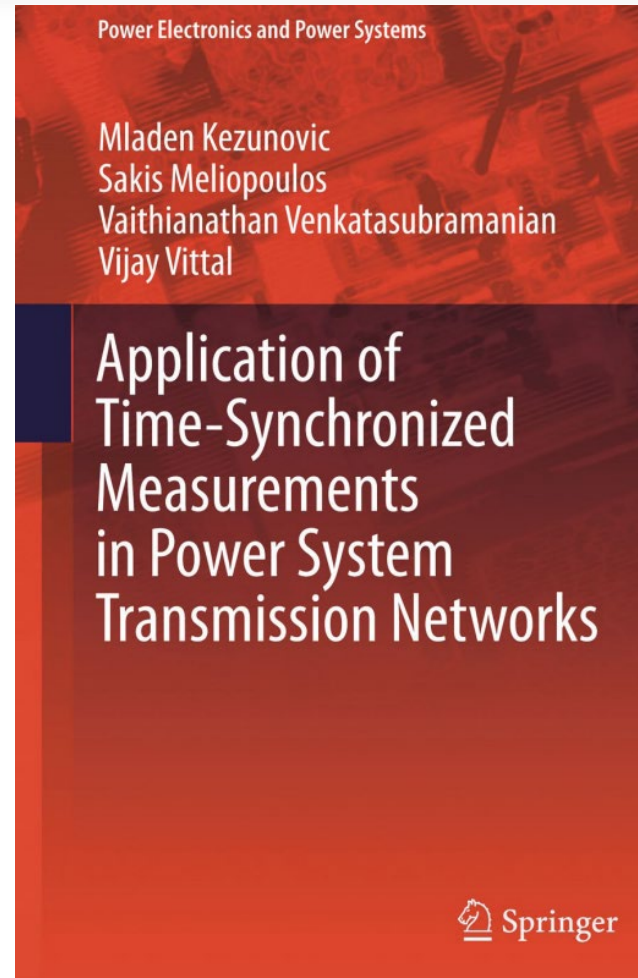
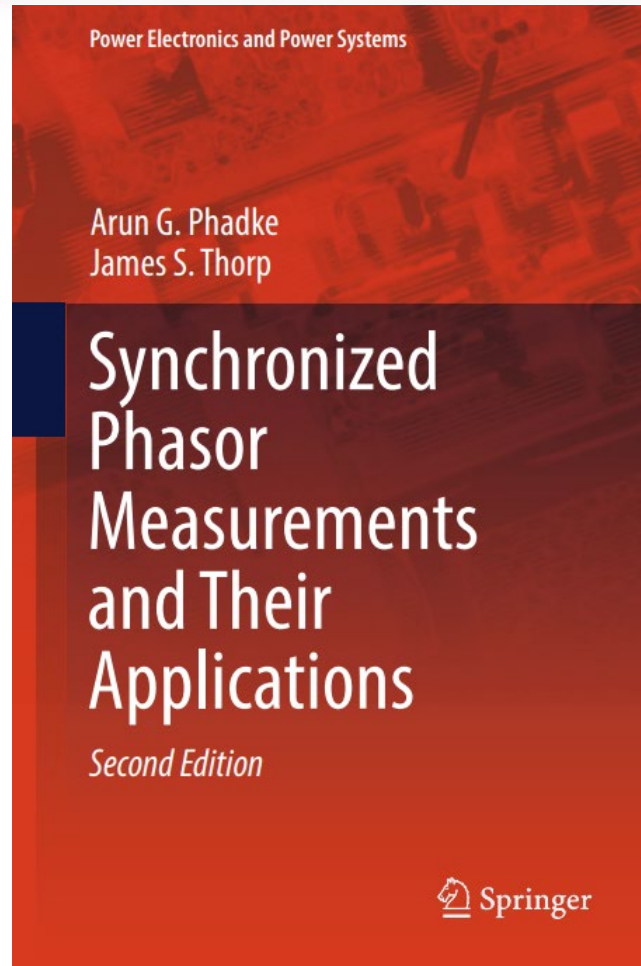
- IEEE C37.118.1
  - class P and class M
- Communication protocols:
  - IEEE C37.118.2
  - IEC 61850-9-2 (SV)
  - DNP/IEC60870-5-101/104
- Time synchronization:
  - IRIG-B
  - PTP IEEE 1588:2008
- Data transferred :
  - V,I,ROCOF (df/dt), f
  - P,Q,S,PF
  - Up to 32DI
- Data Frames:
  - 60 frames/sec on 60Hz
  - 50 frames/sec on 50Hz
- Configuration Frames
  - CFG-1
  - CFG-2
  - CFG-3
- Support form communication
  - TCP – With data reception confirm (delays)
  - UDP – Without data reception confirmation (less reliable)
- NEW!!
  - Data Tags
  - Latitude and Longitude
  - Dual PDC streaming with different rates
- Have Certification from testing laboratory

# PMU30 – Most Advanced PMU



- IEEE C37.118.1
  - class P and class M
- Communication protocols:
  - IEEE C37.118.2
  - IEC 61850-9-2 (SV)
  - DNP/IEC60870-5-101/104
- Time synchronization:
  - IRIG-B
  - PTP IEEE 1588:2019
- Data transferred :
  - V,I,ROCOF (df/dt), f
  - P,Q,S,PF
- Data Frames:
  - 240 frames/sec on 60Hz
  - 200 frames/sec on 50Hz
- Configuration Frames
  - CFG-1
  - CFG-2
  - CFG-3
- Support form communication
  - TCP – With data reception confirm (delays)
  - UDP – Without data reception confirmation (less reliable)
- **NEW!!**
  - Data Tags
  - Latitude and Longitude
  - Dual PDC streaming with different rates
- We are working on Certification

# Recommended literature





**Thank you!**  
**[akorolev@satec-global.com](mailto:akorolev@satec-global.com)**  
**SATEC**  
**Empowering the Grid**  
**[www.satec-global.com](http://www.satec-global.com)**